

Physics & Engineering Mathematics Department Total Marks: 85 Marks



Course Title: Engineering Mathematics (3) b Year: 2nd Computer Engineering and Automatic Control.

Course Code: PME2211 Date: / 6 / 2012 (second term) Allowed time: 3 hrs No. of Pages: (2)

Remarks: (Answer the following questions. Assume any missing data...)

Problem number (1) (25 Marks)

- (a) Given A = 0.2/1 + 0.5/2 + 0.6/3 + 1/4 + 0.7/5 + 0.3/6 + 0.1/7
- (i) Calculate the weak $\alpha cuts$ for $\alpha = 0.4$, 0.6, 0.8
- (ii) Find \overline{A} , CON(A), $A \cap \overline{A}$ and $A \cup \overline{A}$.
- (b) Prove that: If A and B are two fuzzy subsets of the universal set X. Then, the following properties hold for all $\alpha, \beta \in [0,1]$:
- (i) $\alpha \leq \beta$ implies to $A_{\alpha} \supseteq A_{\beta}$
- $(ii) (A \cap B)_{\alpha} = A_{\alpha} \cap B_{\alpha}.$
- (c) Given a fuzzy relations P from A to B defined by:

$$M_P = \begin{bmatrix} 0.4 & 0.8 & 0.5 \\ 0.8 & 0.7 & 0.2 \\ 0.1 & 0.9 & 0.3 \end{bmatrix}$$
, and Q from B to C defined by $M_Q = \begin{bmatrix} 0.1 & 0.8 & 0.2 \\ 0.7 & 0.3 & 0.9 \\ 0.8 & 0.6 & 0.2 \end{bmatrix}$

Find $M_{P \circ Q}$.

(d)Give two deviations between operations on ordinary sets and fuzzy sets. Illustrate your answer by examples.

Problem number (2) (30 Marks)

- (a) If $u(x, y) = x^3 + 6x^2y 3xy^2 2y^3$. Find an analytic function f(z) = u(x, y) + iv(x, y)
- (b) Solve the equation $\cosh z = 0.2$
- (c) Prove that " If f(z) is analytic function in a simply connected domain D and if f'(z) is continuous at each point within and a closed contour C in D, then $\oint f(z) dz = 0$
- (d) Find the general solution of the differential equation:

$$x^{2}y'' - xy' + (x^{2} + 1)y = 0$$

Problem number (3)

30 Marks)

- (a) Find Taylor and Laurent expansions represent the function f(z) and determine the regions of convergence for each with center at $z_0 = 0$ and $f(z) = \frac{z}{5-z}$
- (b) Evaluate the following integrals using complex integration, Gamma and Beta functions:

$$(i) \qquad \oint\limits_{|z|=1} \frac{\cos 2z}{z^4} \, dz$$

(ii)
$$\oint_{|z|=3} \frac{e^{2z} \sinh z}{z^2 + 4} dz$$

$$(iii) \oint_{|z-2|=5/2} \frac{z}{\sin z \ (1+\cos z)} dz$$

(iv)
$$\oint_{|z-2|=1} \frac{\ln z \sinh z^2}{z^4 (z^2 + \pi^2)} dz$$

(v)
$$\oint \frac{e^{iz} + \sin z}{(z - \pi)^9 (z - \pi/2)} dz$$

$$(vi) \quad \int\limits_0^\infty \frac{\cos 5x}{x^4 + 16} \, dx$$

$$(vii) \int_{0}^{\pi/2} (\tan^{3.5}\theta + \tan^{5.5}\theta) e^{-\tan^{2}\theta} d\theta$$
 $(viii) \int_{0}^{2} x^{5} \sqrt{8 - x^{3}} dx$

$$(viii) \quad \int\limits_0^2 x^5 \sqrt{8-x^3} \ dx$$

(ix)
$$\int_{0}^{\infty} \frac{x^{3/2}}{(1+x^2)^7} dx$$

Good luck

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